## CSI 350 Practice Part #4

## 1. Understand $S_{\rm tm}$ .

- (a) What does it mean?
- (b) Which machines belong in it?
- (c) Is it recognizable? If so, provide a recognizer. If not, prove it.

## 2. Understanding $A_{\rm tm}$ .

- (a) What does it mean?
- (b) Which machines belong in it?
- (c) Is it recognizable? If so, provide a recognizer. If not, prove it.
- (d) Is it decidable? If so, provide a decider. If not, prove it.
- 3. Understanding  $HALT_{tm}$ .
  - (a) What does it mean?
  - (b) Which machines belong in it?
  - (c) Is it recognizable? If so, provide a recognizer. If not, prove it.
- 4. Understand countable infinities. Is the set of integers countable? How about the set of all 3D Points?
- 5. Is the power set of the natural numbers countable? (14.3 is very important here)
- 6. Understand the idea of diagonalization (14.1 is a simple version). How does it prove that reals aren't countable? How can we use it to prove 14.3a?
- 7. Understand Reductions (15.1)
  - (a) We can solve A in the presence of B if A reduces to B.
  - (b) If A reduces to B and B is decidable, then A is decidable
  - (c) If A reduces to B and A is undecidable, then B must also be undecidable.
- 8. Questions about TMs (15.2, 15.3, 15.4, 15.5, 15.6, 15.7, 15.8)
  - (a) Is it decidable if a TM ever accepts the string 'a'?
  - (b) What theorem gives us the answer?
  - (c) How do we prove this without the presence of that theorem?
  - (d) Prove it without the theorem.
- 9. What is the class P?

- 10. What is the class NP?
- 11. What is the class PSPACE?
- 12. What is the class NPSPACE?
- 13. What is the relationship between P and NP? ( $P \subseteq NP$ )
- 14. What is the relationship between PSPACE and NPSPACE (PSPACE = NPSPACE)
- 15. How about all P, NP, PSPACE and NPSPACE?